

Q1 a)  $Q = C_1 \Delta V = 6.00 \times 10^{-6} \times 20.0$   
 $= 120 \mu\text{C}$

b) The initial charge on  $C_1$  is now shared between  $C_1$  &  $C_2$

$\therefore Q = Q_1 + Q_2$  —

Also, the voltages on  $C_1$  &  $C_2$  are the same

$\therefore \frac{Q_1}{C_1} = \frac{Q_2}{C_2}$  —

from eqn a)  $Q_1 = \frac{C_1}{C_2} Q_2$

substituting into eqn 1

$Q = Q_2 \left(1 + \frac{C_1}{C_2}\right)$

$\therefore Q_2 = \frac{120 \times 10^{-6}}{1 + \frac{6.00}{3.00}}$   
 $= 40 \mu\text{C}$

and putting this value back into eqn 1

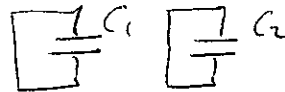
$Q_1 = \frac{6.00}{3.00} \times Q_2$   
 $= 80 \mu\text{C}$

c)  $V = \frac{Q_1}{C_1} = \frac{80 \times 10^{-6}}{6.00 \times 10^{-6}} = \underline{13.3\text{V}}$

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d)

STEP 1: discharge both capacitors



STEP 2: place them in series across  $V$



The capacitors now have equal charges.

Q2 (a) The magnetic flux through the loop is increasing, out of the paper.

By Lenz's Law, the induced emf will therefore cause a magnetic field into the paper.

By the right hand rule, this requires a clockwise current.

$$(b) \frac{d\Phi_B}{dt} = B \frac{dA}{dt} = \underline{Bwv}$$

$$(c) \text{Power} = \frac{\mathcal{E}^2}{R} = \frac{\left(\frac{d\Phi_B}{dt}\right)^2}{R} = \frac{B^2 w^2 v^2}{R}$$

(d) In equilibrium, the input power =  $\frac{\Delta PE}{\Delta t}$  since  $\Delta KE = 0$

$$\therefore \frac{B^2 w^2 v^2}{R} = \frac{d(Mgh)}{dt} = Mg v_T$$

$$= \boxed{v_T = \frac{MgR}{B^2 w^2}}$$

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(e)  $\frac{d\Phi_B}{dt}$  is now  $N$  times greater

The ~~resistance~~ resistance of the loop is now  $N$  times greater, as is the mass

$\therefore$  Power =  $\frac{\mathcal{E}^2}{R}$  goes up by a factor of  $N$

which exactly compensates for the increase in mass

$\therefore$  the ~~value of~~  $v_T$  is unchanged